Chapter- 2 Polynomials

Exerise 2.1

1. The graphs of y = p(x) are given in figure below, for some polynomials p(x). Find the number of zeroes of p(x), in each case.



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- **Sol.** (i) As the graph of polynomial does not meet x-axis, so the polynomial has no zeroes.
 - (*ii*) As the graph of polynomial cuts (meets) x-axis only once, so the polynomial has exactly one zero.
 - (*iii*) As the graph of polynomial cuts (meets) x-axis thrice, so the polynomial has three zeroes.
 - (*iv*) As the graph of polynomial cuts (meets) *x*-axis twice, so the polynomial has exactly two zeroes.
 - (v) As the graph of polynomial cuts (meets) x-axis four times, so the polynomial has four zeroes.
 - (vi) As the graph of polynomial cuts (meets) x-axis three times, so the polynomial has three zeroes.

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Exerise 2.2

1.	Fine	d the zeroes of the following quadratic polynomials and	
	veri	fy the relationship between the zeroes and the	
	coef	ficients.	
	(<i>i</i>)	$x^2 - 2x - 8$ (ii) $4s^2 - 4s + 1$ (iii) $6x^2 - 3 - 7x$	
	(iv)	$4u^2 + 8u$ (v) $t^2 - 15$ (vi) $3x^2 - x - 4$	
Sol.	(i)	Consider polynomial $x^2 - 2x - 8 = (x - 4)(x + 2)$	
		For zeroes, $x - 4 = 0$, $x + 2 = 0$	
		$\Rightarrow x = 4, -2$	
	Zeroes of the polynomial are 4 and -2 .		
	Sum of zeroes = $4 + (-2) = 2$		
	- C $-$ (-2) $-$ Coefficient of x		
		$=$ $\frac{1}{1}$ $=$ $\frac{1}{\text{Coefficient of } x^2}$	
		Product of zeroes = $4 \times (-2) = -8$	
		$=\frac{-8}{-8}$ = Constant term	
		\square Coefficient of x^2	
		Hence verified.	
	(ii)	Consider polynomial $4s^2 - 4s + 1 = (2s - 1)^2$	
		For zeroes, $4s^2 - 4s + 1 = 0$	
		$\therefore \qquad (2s-1)^2 = 0$	
		VEET CV 1	
		$\Rightarrow \qquad 2s-1=0 \Rightarrow s=\frac{1}{2}.$	
		\therefore Polynomial has equal zeroes, <i>i.e.</i> , $\frac{1}{2}$ and $\frac{1}{2}$.	
		Sum of zeroes = $\frac{1}{2} + \frac{1}{2} = 1 = \frac{4}{4}$	
		$= - \frac{(-4)}{4} = - \frac{\text{Coefficient of } s}{\text{Coefficient of } s^2}$	
		Product of zeroes = $\frac{1}{2}$. $\frac{1}{2}$ = $\frac{1}{4}$ = $\frac{\text{Constant term}}{\text{Coefficient of }s^2}$.	
		Hence verified.	
	(iii)	Consider polynomial $6x^2 - 3 - 7x = 6x^2 - 7x - 3$	
		$= 6x^{2} - 9x + 2x - 3 = 3x(2x - 3) + 1(2x - 3)$	
		-(2r-3)(3r+1)	
		$= (\Delta n - 0)(0n + 1)$	

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For zeroes, 2x - 3 = 0, 3x + 1 = 0. $\Rightarrow x = \frac{3}{2}, -\frac{1}{3}$ \Rightarrow Zeroes of polynomial are $\frac{3}{2}$ and $-\frac{1}{3}$. Sum of zeroes = $\frac{3}{2} - \frac{1}{3} = \frac{7}{6} = \frac{-(-7)}{6}$ $= -\frac{\text{Coefficient of } x}{\text{Coefficient of } r^2}$ Product of zeroes = $\frac{3}{2} \times \frac{(-1)}{2}$ $=\frac{-1}{2}=\frac{-3}{6}=\frac{\text{Constant term}}{\text{Coefficient of }x^2}$. Hence verified. (iv) Consider polynomial $4u^2 + 8u = 4u(u + 2)$. 4u(u+2) = 0For zeroes, u = 0 or u + 2 = 0 \Rightarrow Zeroes of the polynomial are 0 and -2. ÷. Sum of zeroes = $0 + (-2) = -2 = \frac{-8}{4}$ $= \frac{-\text{Coefficient of } u}{\text{Coefficient of } u^2}$ Product of zeroes = $0 \times (-2) = 0 = \frac{0}{4}$ $= \frac{\text{Constant term}}{\text{Coefficient of } u^2}$ Hence verified. (v) Consider polynomial $t^2 - 15 = (t - \sqrt{15})(t + \sqrt{15})$ For zeroes, $(t - \sqrt{15}) (t + \sqrt{15}) = 0$ $\Rightarrow t - \sqrt{15} = 0, t + \sqrt{15} = 0$ \Rightarrow $t = \sqrt{15}$, $t = -\sqrt{15}$

 \therefore Zeroes of the polynomial are $\sqrt{15}$ and $-\sqrt{15}$.

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Hence verified.

2. Find a quadratic polynomial each with the given numbers as the sum and product of its zeroes respectively.

(i)
$$\frac{1}{4}$$
, -1 (ii) $\sqrt{2}$, $\frac{1}{3}$ (iii) 0, $\sqrt{5}$
(iv) 1, 1 (v) $-\frac{1}{4}$, $\frac{1}{4}$ (vi) 4, 1.

Sol. (*i*) Let polynomial be $f(x) = ax^2 + bx + c$...(*i*)

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	Sum of zeroes	$=\frac{1}{4}=-\frac{(-1)}{4}=-\frac{b}{a}$	(ii)			
	Product of zeroes	$= -1 = \frac{-4}{4} = \frac{c}{a}$	(<i>iii</i>)			
	From equations (<i>ii</i>) and (<i>iii</i>), we get a = 4, b = -1, c = -4.					
	Substituting these values in equation (i) , we get					
	Polynomial $f(x) = 4x^2 - x - 4$. We can have infinite such polynomials as $f(x) = k(4x - x - 4)$, k is a real number.					
(ii)	Let polynomial be $f(x)$	$= ax^2 + bx + c$	(i)			
	Sum of zeroes	$=\sqrt{2} = -\frac{(-3\sqrt{2})}{3}$				
		$=-\frac{b}{a}$	(ii)			
	Product of zeroes	$=\frac{1}{3}=\frac{c}{a}$	(iii)			
	From equations (ii) and	d (iii), we get				
	a = 3, b	$= -3\sqrt{2}$, $c = 1$.				
	Substituting these values in equation (i), we get					
	Polynomial $f(x) = 3x^2$	$-3\sqrt{2}x + 1.$				
	or $f(x) = k(3x^2 - 3\sqrt{2})$	$\overline{2}x + 1$), k is a real number	er.			
(iii)	Let polynomial be $f(x)$	$= ax^2 + bx + c$	(i)			
	Sum of zeroes	$= 0 = - \frac{(-0)}{1} = - \frac{b}{a}$	(ii)			
	Product of zeroes	$= \sqrt{5} = \frac{\sqrt{5}}{1} = \frac{c}{a}$	(<i>iii</i>)			
	From equations (ii) and	d (iii), we get				
	a = 1, b	$= 0, c = \sqrt{5}$				
	Substituting these values in equation (i) , we get					
	Polynomial $f(x) = x^2 +$	$\sqrt{5}$.				
	or $f(x) = k(x^2 + \sqrt{5})$,	k is a real number.				
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(iv)	Let polynomial be $f(x) = ax^2 + bx + c$	(<i>i</i>)			
	Sum of zeroes $= 1 = \frac{1}{1} = -\frac{(-1)}{1}$				
	$= - \frac{b}{a}$	(ii)			
	Product of zeroes $= 1 = \frac{1}{1} = \frac{c}{a}$	(<i>iii</i>)			
	From equations (<i>ii</i>) and (<i>iii</i>), we get a = 1, b = -1, c = 1. Substituting these values in equation (<i>i</i>), we get				
	Polynomial $f(x) = x^2 - x + 1$.				
	or $f(x) = k(x^2 - x + 1)$, k is a real number.				
(<i>v</i>)	Let polynomial be $f(x) = ax^2 + bx + c$	(i)			
	Sum of zeroes $= -\frac{1}{4} = -\frac{1}{4} = -\frac{b}{a}$	(ii)			
	Product of zeroes $= \frac{1}{4} = \frac{c}{a}$	(<i>iii</i>)			
	From equations (ii) and (iii), we get				
	a = 4, b = 1, c = 1				
	Substituting these values in equation (i) , we get				
	Polynomial $f(x) = 4x^2 + x + 1$.				
	or $f(x) = k(4x^2 + x + 1)$, k is a real number.				
(vi)	Let polynomial be $f(x) = ax^2 + bx + c$	(<i>i</i>)			
	Sum of zeroes $= 4 = -\frac{(-4)}{1} = -\frac{b}{a}$	(ii)			
	Product of zeroes $= 1 = \frac{1}{1} = \frac{c}{a}$	(<i>iii</i>)			
	From equations (<i>ii</i>) and (<i>iii</i>), we get $a = 1, b = -4, a = 1$				
	a = 1, o = -4, c = 1 Substituting these values in equation (<i>i</i>), we get Polynomial $f(x) = x^2 - 4x + 1$				
	or $f(r) = b(r^2 = 4r \pm 1)$ k is a real number				
	(n - n) = n(n - m + 1), n = n = 1				

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Exerise 2.3

1. Divide the polynomial p(x) by the polynomial g(x) and find the quotient and remainder in each of the following: (i) $p(x) = x^3 - 3x^2 + 5x - 3$, $g(x) = x^2 - 2$ (ii) $p(x) = x^4 - 3x^2 + 4x + 5$, $g(x) = x^2 + 1 - x$ (iii) $p(x) = x^4 - 5x + 6$, $g(x) = 2 - x^2$. (i) $p(x) = x^3 - 3x^2 + 5x - 3$ and $g(x) = x^2 - 2$ Sol. $-3x^2 + 7x - 3$ Second term of quotient is $-3x^2$ + 6 $\frac{-}{7x-9}$ + $\frac{-3x^2}{x^2} = -3$ We have quotient q(x) = x - 3 and remainder r(x) = 7x- 9.

(*ii*)
$$p(x) = x^4 - 3x^2 + 4x + 5$$
, $g(x) = x^2 + 1 - x$.
 $x^2 + x - 3$

:. Quotient $q(x) = x^2 + x - 3$; remainder r(x) = 8.

(*iii*)
$$p(x) = x^4 - 5x + 6$$
, $g(x) = 2 - x^2$

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$$\therefore \quad \text{Quotient } q(x) = -x^2 - 2,$$

remainder $r(x) = -5x + 10.$

- **2.** Check whether the first polynomial is a factor of the second polynomial by dividing the second polynomial by the first polynomial:
- (i) $t^2 3$, $2t^4 + 3t^3 2t^2 9t 12$ (ii) $x^2 + 3x + 1$, $3x^4 + 5x^3 - 7x^2 + 2x + 2$ (iii) $x^3 - 3x + 1$, $x^5 - 4x^3 + x^2 + 3x + 1$. Sol. (i) Let $p(t) = 2t^4 + 3t^3 - 2t^2 - 9t - 12$, $g(t) = t^2$ Let us divide p(t) by g(t)

Sol. (i) Let
$$p(t) = 2t + 3t - 2t - 5t - 12$$
, $g(t) = t - 3$
Let us divide $p(t)$ by $g(t)$
 $2t^2 + 3t + 4$

Here, quotient $q(t) = 2t^2 + 3t + 4$, remainder r(t) = 0. As remainder is 0. Hence, $t^2 - 3$ is a factor of the polynomial

 $2t^4 + 3t^3 - 2t^2 - 9t - 12.$

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(ii) Let us divide second polynomial $p(x) = 3x^4 + 5x^3 - 7x^2 + 2x + 2$ by $q(x) = x^2 + 3x + 1$. $3x^2 - 4x + 2$ First term of quotient $=\frac{3x^4}{x^2}=3x^2$ Second term of quotient $=\frac{-4x^3}{x^2} = -4x$ + + + $2x^2 + 6x + 2$ Third term of quotient $2x^2 + 6x + 2$ $=\frac{2x^2}{x^2}=2$ 0 Here, quotient $q(x) = 3x^2 - 4x + 2$, remainder r(x) = 0We have $3x^4 + 5x^3 - 7x^2 + 2x + 2$ $=(x^{2}+3x+1)(3x^{2}-4x+2)+0$ As remainder is zero. Hence, first polynomial is a factor of the second polynomial. (iii) Let $p(x) = x^5 - 4x^3 + x^2 + 3x + 1$, $g(x) = x^3 - 3x + 1$ Let us divide p(x) by q(x). $x^2 - 1$ $x^3 - 3x + 1$ $x^5 - 4x^3 + x^2 + 3x + 1$ First term of quotient $=\frac{x^5}{x^3}=x^2$ Second term of quotient $-x^3 + 3x - 1$ $=\frac{-x^3}{x^3}=-1$ + - + $\mathbf{2}$

> Here, quotient $q(x) = x^2 - 1$, remainder r(x) = 2As remainder is not zero.

Hence, $x^3 - 3x + 1$ is not a factor of $x^5 - 4x^3 + x^2 + 3x + 1$.

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3. Obtain all other zeroes of $3x^4 + 6x^3 - 2x^2 - 10x - 5$, if two of its zeroes are $\sqrt{\frac{5}{3}}$ and $-\sqrt{\frac{5}{3}}$.

Sol. Two zeroes of polynomial $3x^4 + 6x^3 - 2x^2 - 10x - 5$ are

$$x = \sqrt{\frac{5}{3}}$$
 and $x = -\sqrt{\frac{5}{3}}$

: $(\sqrt{3} x - \sqrt{5})$ and $(\sqrt{3} x + \sqrt{5})$ are factors of the polynomial

 $3x^4 + 6x^3 - 2x^2 - 10x - 5$

 $\Rightarrow (\sqrt{3} x - \sqrt{5})(\sqrt{3} x + \sqrt{5}) = 3x^2 - 5 \text{ is a factor of the polynomial}$

$$3x^4 + 6x^3 - 2x^2 - 10x - 5$$

Let us use division algorithm to find other zeroes. Dividing $3r^4 + 6r^3 - 2r^2 - 10r - 5$ by $(3r^2 - 5)$

$$x^{2} + 2x + 1$$

$$3x^{2} - 5 \begin{vmatrix} 3x^{4} + 6x^{3} - 2x^{2} - 10x - 5 \\ 3x^{4} - 5x^{2} \\ - + \end{vmatrix}$$
 First term of quotient
$$3x^{4} - 5x^{2} \\ - + \\ 6x^{3} + 3x^{2} - 10x - 5 \\ 6x^{3} - 10x \\ - + \\ 3x^{2} - 5 \\ - + \\ 0 \end{vmatrix}$$
 Second term of quotient
$$\frac{6x^{3}}{3x^{2}} = 2x$$

Third term of quotient
$$\frac{3x^{2} - 5}{3x^{2}} = 1$$

By division algorithm, we have

$$3x^{4} + 6x^{3} - 2x^{2} - 10x - 5 = (3x^{2} - 5)(x^{2} + 2x + 1)$$
$$= (3x^{2} - 5)(x + 1)^{2}$$

Other zeroes of the polynomial are -1, -1.

[By using x + 1 = 0]

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Hence, zeroes of the polynomial

$$3x^4 + 6x^3 - 2x^2 - 10x - 5$$
 are
 $\sqrt{\frac{5}{3}}, -\sqrt{\frac{5}{3}}, -1$ and -1 .

- **4.** On dividing $x^3 3x^2 + x + 2$ by a polynomial g(x), the quotient and remainder were x 2 and -2x + 4, respectively. Find g(x).
- **Sol.** We have $p(x) = x^3 3x^2 + x + 2$, g(x),

$$q(x) = x - 2$$
 and $r(x) = -2x + 4$.

Using division algorithm, we have

$$p(x) = g(x) \times q(x) + r(x)$$

$$\Rightarrow x^{3} - 3x^{2} + x + 2 = g(x) \times (x - 2) + (-2x + 4)$$

$$\Rightarrow x^{3} - 3x^{2} + x + 2 + 2x - 4 = g(x) \times (x - 2)$$

$$\Rightarrow g(x) \times (x - 2) = x^{3} - 3x^{2} + 3x - 2$$

$$g(x) = \frac{x^{3} - 3x^{2} + 3x - 2}{x - 2}$$

$$r + 1$$

$$x - 2 \qquad x^{3} - 3x^{2} + 3x - 2$$

$$r^{3} - 2x^{2}$$

$$r^{4} - x + 1$$

$$r^{2} + 3x - 2$$

$$r^{2} + 2x$$

$$r^{2} - x^{2} + 2x$$

$$r^{2} - x$$

Hence, $g(x) = x^2 - x + 1$.

- **5.** Give examples of polynomials p(x), g(x), q(x) and r(x), which satisfy the division algorithm and
 - (i) $deg \ p(x) = deg \ q(x)$ (ii) $deg \ q(x) = deg \ r(x)$

(iii)
$$deg r(x) = 0$$

Sol. (i) Let
$$p(x) = 3x^2 + 6x - 11$$
 and $g(x) = 3$

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Then $q(x) = x^2 + 2x - 3$, r(x) = -2Here, deg p(x) = deg q(x)

- (*ii*) Let $p(x) = x^3 + 6x^2 + 5x$ and $g(x) = x^2 + 2$ Then q(x) = x + 6, r(x) = -x - 12Here, deg q(x) = deg r(x).
- (*iii*) Let $p(x) = 3x^3 + 5x^2 6x + 7$ and g(x) = x 1Then $q(x) = 3x^2 + 8x + 2$, r(x) = 9Here, deg r(x) = 0**Note:** Each of (*i*), (*ii*) and (*iii*) has several examples.



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Exerise 2.4

1. Verify that the numbers given alongside of the cubic polynomials below are their zeroes. Also verify the relationship between the zeroes and the coefficients in each case:

_

(i)
$$2x^3 + x^2 - 5x + 2; \frac{1}{2}, 1, -2$$

(ii) $x^3 - 4x^2 + 5x - 2; 2, 1, 1$
Sol. (i) Let $p(x) = 2x^3 + x^2 - 5x + 2$
If $\frac{1}{2}$, 1, -2 are zeroes of $p(x)$, then
 $p\left(\frac{1}{2}\right) = 0, p(1) = 0$ and $p(-2) = 0$.
Let us verify.
 $p\left(\frac{1}{2}\right) = 2\left(\frac{1}{2}\right)^3 + \left(\frac{1}{2}\right)^2 - 5 \times \frac{1}{2} + 2$
 $= \frac{2}{8} + \frac{1}{4} - \frac{5}{2} + 2$
 $= \frac{2+2-20+16}{8} = \frac{0}{8} = 0.$
 $p(1) = 2(1)^3 + (1)^2 - 5(1) + 2 = 2 + 1 - 5 + 2 = 2$

$$p(1) = 2(1)^{3} + (1)^{2} - 5(1) + 2 = 2 + 1 - 5 + 2 = 0.$$

$$p(-2) = 2(-2)^{3} + (-2)^{2} - 5 \times (-2) + 2$$

$$= -16 + 4 + 10 + 2 = 0$$

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Hence, we can say $\alpha = \frac{1}{2}$, $\beta = 1$, $\gamma = -2$ are zeroes of p(x). **Relationship:** $\alpha + \beta + \gamma = \frac{1}{2} + 1 - 2 = \frac{1}{2} - 1 = -\frac{1}{2}$ $= \frac{-\text{Coefficient of } x^2}{\text{Coefficient of } r^3}$ $\alpha\beta + \beta\gamma + \gamma\alpha = \frac{1}{2} \times 1 + 1 \times (-2) + (-2) \times \frac{1}{2}$ $=\frac{1}{2} + (-2) - 1 = -\frac{5}{2} = -\frac{5}{2}$ $= \frac{\text{Coefficient of } x}{\text{Coefficient of } x^3}$ $\alpha\beta\gamma = \frac{1}{2} \times 1 \times (-2) = -1 = -\frac{(2)}{2}$ and $= - \frac{\text{Constant term}}{\text{Coefficient of } x^3}.$ Hence, relationship is verified. (*ii*) Let $q(x) = x^3 - 4x^2 + 5x - 2$ If 2, 1 and 1 are zeroes of q(x), then q(2) = 0 and q(1) = 0.Let us verify. Now $q(2) = (2)^3 - 4(2)^2 + 5(2) - 2 = 0 = 8 - 16 + 10 - 2 = 0$ $a(1) = (1)^3 - 4(1)^2 + 5(1) - 2 = 1 - 4 + 5 - 2 = 0$ Hence, verified. Let $\alpha = 2$, $\beta = 1$, $\gamma = 1$. **Relationship:** Sum of zeroes = $\alpha + \beta + \gamma = 2 + 1 + 1 = 4$ $= -\frac{(-4)}{1} = -\frac{\text{Coefficient of } x^2}{\text{Coefficient of } x^3}$ Sum of product of zeroes taken in pair $= \alpha\beta + \beta\gamma + \gamma\alpha = 2 + 1 + 2 = 5$ $=\frac{5}{1}=\frac{\text{Coefficient of }x}{\text{Coefficient of }r^3}$

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Product of zeroes =
$$\alpha\beta\gamma = 2 = \frac{2}{1} = -\frac{(-2)}{1}$$

Constant term

 $= - \frac{\text{Constant term}}{\text{Coefficient of } x^3}$

Hence, relationship is verified.

- Find a cubic polynomial with the sum, sum of the product of its zeroes taken two at a time, and the product of its zeroes as 2, -7, -14 respectively.
- **Sol.** Let polynomial be $f(x) = ax^3 + bx^2 + cx + d$...(*i*) Let α , β and γ be the zeroes of the polynomial

Given,
$$\alpha + \beta + \gamma = 2 = \frac{-(-2)}{1} = -\frac{b}{a}$$
 ...(*ii*)

$$\alpha\beta + \beta\gamma + \gamma\alpha = -7 = \frac{-7}{1} = \frac{c}{a} \qquad \dots (iii)$$

$$\alpha\beta\gamma = -14 = -\frac{14}{1} = -\frac{d}{a}$$
 ...(*iv*)

From (*ii*), (*iii*) and (*iv*), we have a = 1, b = -2, c = -7, d = 14.Substituting these values in (*i*), we get $f(x) = x^3 - 2x^2 - 7x + 14$ or $f(x) = k(x^3 - 2x^2 - 7x + 14),$

3. If the zeroes of the polynomial $x^3 - 3x^2 + x + 1$ are a - b, a, a + b, find a and b.

Sol. Let the given polynomial be $Ax^3 + Bx^2 + Cx + D$ Here, A = 1, B = -3, C = 1, D = 1Zeroes are a - b, a and a + b.

Sum of zeroes
$$= -\frac{B}{A}$$

 $\Rightarrow \quad a - b + a + a + b = 3$
 $\Rightarrow \quad 3a = 3 \qquad \Rightarrow \quad a = 1.$
Product of zeroes $= -\frac{D}{A}$
 $\Rightarrow \quad (a - b) \ a \ (a + b) = -\frac{1}{1}$
 $\Rightarrow \quad (1 - b) \ . \ 1 \ . \ (1 + b) = -1$

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where k is a real number.

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	\Rightarrow	$1 - b^2 = -1$					
	\Rightarrow	$b^2 = 2 \implies b = \pm$	$\sqrt{2}$				
4.	Hence, a If two ze	$a = 1, b = \pm \sqrt{2}$. eroes of the polynomial $x^4 - 6$	$\delta x^3 - 26x^2 + 138x$				
	– 35 are	$2~\pm~\sqrt{3}$, find other zeroes.					
Sol.	Given polynomial $p(x) = x^4 - 6x^3 - 26x^2 + 138x - 35$						
	As two z	zeroes are $x = 2 \pm \sqrt{3}$.					
	So, $\{x - (2 + \sqrt{3})\}$ $\{x - (2 - \sqrt{3})\}$ is a factor of $p(x)$.						
	<i>i.e.</i> , (x ²	-4x + 1) is a factor of $p(x)$.					
		$r^2 - 2r - 35$					
x ² -	-4x + 1	$ \begin{array}{r} x^{4} - 6x^{3} - 26x^{2} + 138x - 35 \\ x^{4} - 4x^{3} + x^{2} \\ - + - \\ - 2x^{3} - 27x^{2} + 138x - 35 \\ - 2x^{3} + 8x^{2} - 2x \\ + - + \\ - 35x^{2} + 140x - 35 \\ - 35x^{2} + 140x - 35 \\ + - + \\ \hline 0 \end{array} $	First term of quotient $= \frac{x^4}{x^2} = x^2$ Second term of quotient $= \frac{-2x^3}{x^2} = -2x$ Third term of quotient $= \frac{-35x^2}{x^2} = -25$				
	$\mathbf{r}(\mathbf{x})$	$-(m^2 - 4m + 1)(m^2 - 2m - 25)$	$= x^2 = -35$				
	$\therefore p(x) = (x^2 - 4x + 1)(x^2 - 2x - 35)$						
	For othe	r zeroes, $x^2 - 2x - 35 = 0$.					
	\Rightarrow	x - 7x + 5x - 55 = 0					
	\rightarrow	x(x - 7) + 5(x - 7) = 0 (x + 5)(x - 7) = 0					
	\rightarrow	x + 5 = 0, x - 7 = 0					
	\Rightarrow	x = -5.7					
	Hence, o	ther zeroes are -5 and 7.					

5. If the polynomial $x^4 - 6x^3 + 16x^2 - 25x + 10$ is divided by another polynomial $x^2 - 2x + k$, the remainder comes out to be x + a, find k and a.

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Sol.	When	$x^4 - 6x^3 + 16x^2 - 25x + 10$ is divid	ed by $x^2 - 2x$			
	+ k, re	emainder is $x + a$.				
	Using	division algorithm,				
	$x^4 - 6$	$3x^3 + 16x^2 - 25x + 10 = (x^2 - 2x + k) q$	q(x) + (x + a),			
	where	q(x) is quotient.				
	$\Rightarrow x^4$	$- 6x^3 + 16x^2 - 26x + (10 - a) = (x^2 - a)^2 - (10 - a$	2x + k) q(x)			
	$\Rightarrow x^2 - 2x + k$ is a factor of $x^4 - 6x^3 + 16x^2 - 26$					
	-a).		First term			
		$x^2 - 4x + (8 - k)$	of quotient			
<i>x</i> ² –	2x + k	$x^{4} - 6x^{3} + 16x^{2} - 26x + (10 - a)$ $x^{4} - 2x^{3} + kx^{2}$	$= \frac{x^4}{x^2} = x^2$			
		$ \begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$	Second term of quotient $= \frac{-4x^{3}}{x^{2}}$ $= -4x$ Third term of quotient $= \frac{(8-k)x^{2}}{2}$			
			x = (8 - k)			

As remainder is zero,

 $\begin{array}{rl} \therefore & (-10+2k)x + (k^2 - 8k + 10 - a) = 0 \\ \therefore & -10 + 2k = 0 \text{ and } k^2 - 8k + 10 - a = 0 \\ \Rightarrow & k = 5 \text{ and } 25 - 40 + 10 - a = 0 \\ \Rightarrow & k = 5 \text{ and } a = -5. \end{array}$