#### Exerise 9.1

- 1. A circus artist is climbing a 20 m long rope, which is tightly stretched and tied from the top of a vertical pole to the ground. Find the height of the pole, if the angle made by the rope with the ground level is 30° (see figure).
  Sol. Let height of the pole AB = x m Length of the rope AC = 20 m In ΔABC, ∠ACB = 30°
  ∴ sin 30° = AB/AC ⇒ 1/2 = x/20 ⇒ x = 10 m
  - $\therefore$  Height of the pole = 10 m.
  - 2. A tree breaks due to storm and the broken part bends so that the top of the tree touches the ground making an angle 30° with it. The distance between the foot of the tree to the

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point where the top touches the ground is 8 m. Find the height of the tree.

**Sol.** Let the height of tree before storm be AB. Due to storm it breaks from C such that its top A touches the ground at D and makes an angle of  $30^{\circ}$ .

Let AC, *i.e.*, DC = x and BC = y; BD = 8 m [Given]  $\therefore$  Height of tree = x + y ...(*i*)

In  $\triangle BCD$ ,



**3.** A contractor plans to install two slides for the children to play in a park. For the children below the age of 5 years, she prefers to have a slide whose top is at a height of 1.5 m, and is inclined at an angle of  $30^{\circ}$  to the ground, whereas for elder children, she wants to have a steep slide at a height of 3 m, and inclined at an angle of  $60^{\circ}$  to the ground. What should be the length of the slide in each case?

#### Sol. For children below 5 years:

Let *x* m be the length of the slide AC and height AB = 1.5 m [Given].

In 
$$\triangle ABC$$
,  $\angle C = 30^{\circ}$   
 $\therefore \quad \frac{AB}{AC} = \sin 30^{\circ} \implies \frac{1.5}{x} = \frac{1}{2} \begin{bmatrix} x \\ 1.5 \\ B \end{bmatrix}$ 

:. Length of the slide for children below 5 years = 3 m.

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- :. Length of the slide for elder children = 3.46 m.
- **4.** The angle of elevation of the top of a tower from a point on the ground, which is 30 m away from the foot of the tower, is 30°. Find the height of the tower.
- **Sol.** Let AB be the tower and C be a point on the ground such that BC = 30 m. Also let AB = x m. The angle of elevation of the top A from C is 30°.

So, in right-angled  $\triangle ABC$ ,

$$\frac{AB}{BC} = \tan 30^{\circ} \implies \frac{x}{30} = \frac{1}{\sqrt{3}}$$

$$\Rightarrow x = \frac{30}{\sqrt{3}} = 10\sqrt{3} = 10 \times 1.732 = 17.32 \text{ m}$$

Hence, height of the tower is 17.32 m.

- **5.** A kite is flying at a height of 60 m above the ground. The string attached to the kite is temporarily tied to a point on the ground. The inclination of the string with the ground is 60°. Find the length of the string, assuming that there is no slack in the string.
- **Sol.** Let P be the temporarily position of the kite of which string is tied to a point O on the ground. Such that  $\angle POQ$  is 60°, where Q is the point on the ground just below P. Therefore, PQ = 60 m. In  $\triangle POQ$ ,



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$$\frac{OP}{PQ} = \operatorname{cosec} \ 60^{\circ}$$
$$\Rightarrow \quad \frac{x}{60} = \frac{2}{\sqrt{3}} \quad \Rightarrow \quad x = \frac{120}{\sqrt{3}} = 40\sqrt{3} \quad \text{m}$$

Hence, length of the string is  $40\sqrt{3}$  m.

- **6.** A 1.5 m tall boy is standing at some distance from a 30 m tall building. The angle of elevation from his eyes to the top of the building increases from  $30^{\circ}$  to  $60^{\circ}$  as he walks towards the building. Find the distance he walked towards the building.
- Sol. Let a 1.5 m tall boy DP finds the angle of elevation to the top A of the building A.

Let DCB be the horizontal eye sight. When that boy walks towards the building finds increased angle of  $60^{\circ}$  at C.

Given: AQ = 30 m.

$$\begin{array}{c|c} D & T & T \\ 1.5 m & X & C & Y \\ P & Q \\ \end{array}$$

30°

$$AB = AB - BQ = (30 - 1.5) m = 28.5 m.$$

In right-angled  $\triangle ABC$ ,

$$\frac{BC}{AB} = \cot 60^{\circ} \implies \frac{y}{28.5} = \frac{1}{\sqrt{3}}$$
$$\implies y = \frac{28.5}{\sqrt{3}} = 16.45 \text{ m} \qquad \dots(i)$$

In right-angled  $\Delta$  ABD,

$$\frac{\text{BD}}{\text{AB}} = \cot \ 30^{\circ} \implies \sqrt{3} = \frac{x+y}{28.5}$$

$$\Rightarrow x + y = 28.5 \times \sqrt{3} = 49.36 \text{ m}$$

Putting from (i), we get

 $\Rightarrow$  x = (49.36 - 16.45) m = 32.91 m.

Hence, the distance he walked towards the building is 32.91 m.

7. From a point on the ground, the angles of elevation of the bottom and the top of a transmission tower fixed at the top

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30 m

of a 20 m high building are  $45^{\circ}$  and  $60^{\circ}$  respectively. Find the height of the tower.

**Sol.** Let AD be the transmission tower fixed at the top A of the building BA of 20 m high. Angles of elevation of A and D from a point C on the ground are  $45^{\circ}$  and  $60^{\circ}$  respectively, *i.e.*,  $\angle ACB = 45^{\circ}$  and  $\angle DCB = 60^{\circ}$  Let AD = x m and BC = y m

In right-angled  $\triangle ABC$ ,

$$\frac{BC}{AB} = \cot 45^{\circ} \implies \frac{y}{20} = 1 \implies y = 20 \qquad \dots(i)$$
  
In right  $\triangle DBC$ ,  $\frac{DB}{BC} = \tan 60^{\circ}$   
 $\implies \frac{x+20}{y} = \sqrt{3} \implies x+20$   
 $= \sqrt{3} y \qquad \dots(ii)$   
From (i) and (ii), we get  
 $x + 20 = 20 \sqrt{3}$   
 $\implies x = 20 \sqrt{3} - 20 = 20(1.732 - 1) = 14.64 \text{ m}$ 

Hence, the height of the tower is 14.64 m.

- 8. A statue, 1.6 m tall, stands on the top of a pedestal. From a point on the ground, the angle of elevation of the top of the statue is 60° and from the same point the angle of elevation of the top of the pedestal is 45°. Find the height of the pedestal.
- **Sol.** Let height of pedestal AB = x m. Height of statue BC = 1.6 m

 $\angle AOB = 45^{\circ}, \ \angle AOC = 60^{\circ}$ 

In right-angled  $\triangle OAB$ ,

$$\frac{OA}{AB} = \cot 45^{\circ}$$

$$O^{A}_{A5^{\circ}} = 1 \implies OA = x$$

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С

В

xm

...(*i*)

1.6 m

Also in right-angled triangle OAC,

$$\frac{OA}{AC} = \cot \ 60^{\circ} \implies \frac{x}{x+1.6} = \frac{1}{\sqrt{3}} \qquad [From \ (i)]$$
  
$$\implies \sqrt{3} \ x = x + 1.6 \implies (\sqrt{3} - 1)x = 1.6$$
  
$$x = \frac{1.6}{\sqrt{3} - 1} = \frac{1.6(\sqrt{3} + 1)}{2} = 0.8(\sqrt{3} + 1) \ m$$

:. Height of pedestal =  $0.8(\sqrt{3} + 1)$  m or 2.19 m.

- **9.** The angle of elevation of the top of a building from the foot of the tower is 30° and the angle of elevation of the top of the tower from the foot of the building is 60°. If the tower is 50 m high, find the height of the building.
- **Sol.** In the figure, CD is a tower of 50 m high and AB is a building.



**10.** Two poles of equal heights are standing opposite each other on either side of the road, which is 80 m wide. From a point between them on the road, the angles of elevation of the top of the poles are 60° and 30°, respectively. Find the

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heights of the poles and the distances of the point from the poles.

**Sol.** Let height of the each pole = h m.



Let BE = x m, ED = (80 - x) m.

 $\angle AEB = 60^\circ, \angle CED = 30^\circ$ 

In right-angled triangle ABE,

$$\frac{\text{AB}}{\text{BE}} = \tan 60^\circ \implies \frac{h}{x} = \sqrt{3} \implies h = \sqrt{3} x \quad ...(i)$$

In right-angled triangle CDE,

$$\frac{\text{CD}}{\text{DE}} = \tan 30^{\circ}$$

$$\frac{h}{80 - x} = \frac{1}{\sqrt{3}} \implies h = \frac{80 - x}{\sqrt{3}} \qquad \dots (ii)$$

From (i) and (ii), we get

$$\sqrt{3} x = \frac{80 - x}{\sqrt{3}} \implies 3x = 80 - x$$

 $\Rightarrow \qquad 4 \ x = 80 \qquad \Rightarrow \qquad x = 20 \ \mathrm{m}$ 

:. Distance of the point from one pole = 20 m. Substituting in (i), we get

$$h = 20\sqrt{3}$$
 m

- :. Height of each pole =  $20\sqrt{3}$  m.
- 11. A TV tower stands vertically on a bank of a canal. From a point on the other bank directly opposite the tower, the angle of elevation of the top of the tower is  $60^{\circ}$ . From another point 20 m away from this point on the line joining this point to the foot of the tower, the angle of elevation of the top of the tower is  $30^{\circ}$  (see figure). Find the height of the tower and the width of the canal.

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**Sol.** Let width (BC) of the canal is x m and height (AB) of the tower is h m.

In right-angled triangle ABC,

$$\frac{AB}{BC} = \tan 60^{\circ} \implies \frac{h}{x} = \sqrt{3} \implies h = \sqrt{3} x \quad ...(i)$$
  
right-angled triangle ABD,  
$$\frac{AB}{BD} = \tan 30^{\circ} \implies \frac{h}{20+x} = \frac{1}{\sqrt{3}}$$

$$h = \frac{20 + x}{\sqrt{3}}$$

In

 $\Rightarrow$ 

 $\Rightarrow$ 

From (i) and (ii), we get

$$\sqrt{3} x = \frac{20 + x}{\sqrt{3}} \implies 3x = 20 + x$$
$$2x = 20 \implies x = 10 \text{ m}$$

 $\therefore$  Width of the canal = 10 m.

Substituting in (i), we get  $h = 10\sqrt{3}$  m

- :. Height of the TV tower =  $10\sqrt{3}$  m.
- 12. From the top of a 7 m high building, the angle of elevation of the top of a cable tower is  $60^{\circ}$  and the angle of depression of its foot is  $45^{\circ}$ . Determine the height of the tower.
- **Sol.** In the figure, AB represents a 7 m high building and PQ represents a cable tower. Angle of elevation to the top P from A is  $60^{\circ}$  and angle of depression to the bottom Q from same point A is  $45^{\circ}$ .

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8

...(*ii*)

So,  $\angle PAR = 60^{\circ}$  and  $\angle RAQ = 45^{\circ} = \angle AQB$ . Let AB = 7 m = QR, AR = BQ = x m and PR = y mIn rt  $\triangle ABQ$ ,  $\frac{AB}{BQ} = \tan 45^{\circ} \Rightarrow \frac{7}{x} = 1$   $\Rightarrow x = 7 \text{ m} \dots(i)$ In rt  $\triangle PRA$ ,  $\frac{PR}{AR} = \tan 60^{\circ} \Rightarrow \frac{y}{x} = \sqrt{3}$   $\Rightarrow y = \sqrt{3} x = 7\sqrt{3} \text{ m}$  [From (i)]  $\therefore$  Height of the tower =  $7 + y = (7 + 7\sqrt{3}) \text{ m}$ 

Eight of the tower =  $7 + y = (7 + 7\sqrt{3})$  in

= 
$$7(1 + \sqrt{3})$$
 m =  $7 \times 2.732$  m  
= 19.12 m.

- 13. As observed from the top of a 75 m high lighthouse from the sea-level, the angles of depression of two ships are  $30^{\circ}$  and  $45^{\circ}$ . If one ship is exactly behind the other on the same side of the lighthouse, find the distance between the two ships.
- **Sol.** In the figure, AB represents a 75 m high lighthouse, C and D are the positions of two ships where angles of depression from top of the tower are 45° and 30° respectively.

Let BC = x m and BD = y m.

We have to find the distance between the two ships,

*i.e.*, 
$$CD = BD - BC = y - x$$

In right-angled  $\triangle ABC$ ,

$$\frac{BC}{AB} = \cot 45^{\circ}$$

$$\Rightarrow \frac{x}{75} = 1$$

$$\Rightarrow x = 75 \text{ m}$$
In right-angled  $\triangle ABD$ ,
$$\frac{BD}{AB} = \cot 30^{\circ} \Rightarrow \frac{y}{75} = \sqrt{3}$$

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$$\Rightarrow$$
  $y = 75\sqrt{3}$  m

The distance between two ships ....

$$= y - x = 75\sqrt{3} - 75 = 75(\sqrt{3} - 1)$$
 m.

**14.** A 1.2 m tall girl spots a balloon moving with the wind in a horizontal line at a height of 88.2 m from the ground. The angle of elevation of the balloon from the eyes of the girl at any instant is 60°. After some time, the angle of elevation reduces to 30° (see Fig.). Find the distance travelled by the balloon during the interval.



Sol. When the horizontally moving balloon is at P, a girl AB (say) finds  $\angle PAC$  is 60° and at the position R,  $\angle RAD$  is 30°.

We have to find the distance travelled in horizontal line, i.e., PR or CD.

Р

Consider PC = PQ - CQ = (88.2 - 1.2) m = 87 m = RDIn rt  $\triangle ACP$ ,

tan 
$$60^{\circ} = \frac{PC}{AC}$$
  
 $\Rightarrow \sqrt{3} = \frac{87}{AC}$   
 $\Rightarrow AC = \frac{87}{\sqrt{3}}$   
In  $\triangle ADR$ ,  
tan  $30^{\circ} = \frac{RD}{AD} \Rightarrow \frac{1}{\sqrt{3}} = \frac{87}{AD} \Rightarrow AD = 87\sqrt{3}$  ...(*ii*)

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Now CD = AD - AC

$$= 87\sqrt{3} - \frac{87}{\sqrt{3}} = 87\frac{(3-1)}{\sqrt{3}} = \frac{87\times2}{\sqrt{3}} \times \frac{\sqrt{3}}{\sqrt{3}}$$
  
[From (i) and (ii)]

 $= 29 \times 2 \times \sqrt{3} = 58\sqrt{3}$ 

- $\therefore$  The distance travelled by the balloon during the interval is  $58\sqrt{3}$  m.
- **15.** A straight highway leads to the foot of a tower. A man standing at the top of the tower observes a car at an angle of depression of 30°, which is approaching the foot of the tower with a uniform speed. Six seconds later, the angle of depression of the car is found to be 60°. Find the time taken by the car to reach the foot of the tower from this point.
- Sol. Let AB be the tower on the top of which a man is standing and finds angle of depression to the position D of the running car as  $30^{\circ}$ .

After 6 seconds, angle is found  $60^{\circ}$  at C.

Let AB = h m, DC = x m and BC = y m.

When car is at D:

$$\frac{x+y}{h} = \cot 30^{\circ}$$

 $\Rightarrow x + y = \sqrt{3} h \qquad \dots(i)$ When car is at C:

$$\frac{y}{h} = \cot 60^\circ \implies \frac{y}{h} = \frac{1}{\sqrt{3}} \implies h = \sqrt{3} y \qquad ...(ii)$$

์ 30°

**x**m

60° <sup>(30°</sup>

<u>∕</u>60° C v

vm

hm

From (i) and (ii), we have

$$x + y = \sqrt{3} \cdot \sqrt{3} y = 3y \implies x = 2y \implies y = \frac{x}{2}$$

 $\therefore$  Distance *x* is covered in 6 seconds

 $\therefore$  Distance y, *i.e.*,  $\frac{x}{2}$  is covered in 3 seconds.

16. The angles of elevation of the top of a tower from two points at a distance of 4 m and 9 m from the base of the tower

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and in the same straight line with it are complementary. Prove that the height of the tower is 6 m.

Sol. In the drawn figure, AB represents a tower, C and D are two points distant 4 m and 9 m away from the base B. Let angle of elevation to the top A from C is  $\alpha$  and from D is  $90^{\circ} - \alpha$ . A

In right-angled AABC

In right angled Linbo,  

$$\frac{h}{4} = \tan \alpha \qquad ...(i)$$
In right-angled  $\triangle ABD$ ,  

$$\frac{h}{9} = \tan (90^{\circ} - \alpha)$$

$$\Rightarrow \qquad \frac{h}{9} = \cot \alpha \qquad ...(ii)$$
Multiplying the corresponding sides of (i) and (ii), we get  

$$\frac{h}{4} \cdot \frac{h}{9} = \tan \alpha \cdot \cot \alpha \Rightarrow \frac{h^2}{36} = 1$$

$$\Rightarrow \qquad h^2 = 36 \qquad \Rightarrow \qquad h = 6$$

Height of the tower = 6 m. Hence proved. ...

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